

<http://fermatstheorem.blogspot.com/2005/07/eisenstein-integers.html>

Elliptic (L) functions; Elliptic Elliptic curves

The proof

NOVA video 1997

Andrew Wiles became obsessed with Fermat's last theorem

Fermat's rule:

$x^n + y^n = z^n$  not equal to  $z^n$  for  $n$  greater than 2

He said he had a proof, but the proof was never found

For 150 years, mathematicians tried to prove it.

Many mathematicians assumed that the proof was unimportant;

Did not lead to anything. Wiles gave up on the proof and worked with his advisor on elliptic curves, the in thing to study. Elliptic curves are very important; they are not elliptic; they are a cubic curve whose solutions looks like a donut **torus**? Every point on the donut is a solution to an equation. (3 D)

In China, Fermat's theorem and elliptic curves were becoming inextricably linked.

Then, two Chinese mathematicians Goro Shimura and Taniyama worked together.

Taniyama made productive mistakes. Together they worked on the math of modular functions. There are five fundamental math operations: add, sub, mult, div, and modular forms. Modular functions are on complex plane that are inordinately symmetrical. They satisfy so many conditions of symmetry that their existence seem like accidents. They exist in hyperbolic space ? modular forms would seem to have nothing to do with the world of elliptic curves.

In an international symposium in 1955, Taniyama proposed a number of problems that led to the claim that every elliptic curve is really a modular form in disguise. This became known as the Taniyama Shimura conjecture. "every rational elliptic is modular". By 1969, people were coming to believe the conjecture. Other theories developed which were based on the original TS conjecture. Taniyama committed suicide in 1958. TS conjecture went on to become a great unproven conjecture. At first no one had any idea that TS had anything to do with Fermat's last theorem, but that changed in the 80s. In 1985, the German mathematician Gerhard Frey (Eve Eleguah) had an idea.

What if Fermat was wrong, and there were solutions for higher orders? Frey found that starting with a fictitious solution

(Is it a solution or not?)

to Fermat's equation led to an elliptic curve with some weird properties. That elliptic curve seems to not be modular, but TS says all elliptic curves are modular. So "if Fermat is wrong, then so is TS; but if TS is correct, then so is Fermat." But Frey did not prove his fictitious elliptic curve solution was not modular. Frey's theory became known as the epsilon conjecture. The epsilon conjecture was said to be proved; ie it was proved that this fictitious solution was not modular.

So the epsilon conjecture was proved, so now Wiles says he just has to show that TS is correct to show Fermat is correct.

But "if Fermat is wrong, then so is TS; but if TS is correct, then so is Fermat" Does not make any sense, because by coming up with the fictitious solution, Fry showed that Fermat was incorrect.

Wiles tries to show there are the same number of modular functions and elliptic equations; both are infinite, but can count "packets"; can count elliptic equations, but finds a Galois representation of the elliptic equations, whose packets can be counted.

Wiles hoped Iwasawa theory could help him complete his counting strategy by calculating a class number formula, but he got stuck.  
Ended up using a class number formula developed by a student of Coates, Flach & Kolyagin. Wiles then proved Kolyagin's class number formula.

Error found in Flach Kolyagin class number formula step.  
From Flach Kolyagin was able to rework his original Iwasawa theory.\

So now TS and Fermat's last theorem are considered proven.

Contributions from Dozens of mathematicians.